

**Exam 2**  
**Chapter 2.2-2.5 and 3**

Name: \_\_\_\_\_

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Do not write your name on any other page. Answer the following questions. *Answers without proper evidence of knowledge will not be given credit.* Make sure to make reasonable simplifications. Do not approximate answers. Give exact answers. **Only scientific calculators are allowed on this exam.**

**Show your work!**

1. (10 points) Draw the phase diagram for the autonomous differential equation

$$\frac{dx}{dt} = x^2 - 5x + 4$$

and determine which critical points are stable and unstable.

**2.** (10 points) Consider a body that moves horizontally through a medium whose resistance is proportional to the square of velocity so that

$$\frac{dv}{dt} = -2v^2.$$

Assuming that  $v(0) = 1$  and  $x(0) = 1$ , find the position  $x(t)$  as a function of  $t$ .

**3.** (10 points) Find the general form of the complementary solution of the differential equation

$$6y^{(4)} + 5y^{(3)} + 25y'' + 20y' + 4 = 0$$

which has characteristic function

$$(r^2 + 4)(6r^2 + 5r + 1) = 0.$$

4. (10 points) Find the particular solution to the differential equation

$$y'' + 2y' + 2y = 3x^2 - 1.$$

5. (10 points) Consider an RLC circuit with  $R = 40$  ohms,  $L = 10$  henries,  $C = 0.02$  farads and  $E(t) = 50 \sin 2t$  volts at time  $t$ . This information gives the differential equation

$$10I'' + 40I' + 50I = 100 \cos 2t$$

for the current  $I(t)$  (in amperes). Find the general complementary solution and the particular solution for this circuit.